

Physics 331 Final Exam Second Semester 2016/2017 Instructor: Abdallah Sayyed-Ahmad

Sunday 4/6/2017

(1) Two uniform infinite sheets of electric charge densities $+\sigma$ and $-\sigma$ intersects at a right angle.

- (a) Find the magnitude the electric field everywhere (5%).
- (b) Determine the direction of the electric field everywhere by sketching the field lines (5%).
- (2) According to quantum mechanics, the electron cloud for a hydrogen atom in the ground state has a charge density $\rho(r) = \frac{e}{\pi a^3} \exp\left(-\frac{2r}{a}\right)$. Where *e* is the charge of the electron and *a* is the Bohr radius.
 - (a) Find the magnitude of the electric field E(r) (10%).
 - (b) Estimate the polarizability (by expanding the exponential assuming $r \ll a$) (10%).
- (3) Two infinite insulated conducting planes maintained at a potential 0 and V_0 form a wedge shaped configuration as shown in the figure. Determine the potential distribution for the region $0 < \phi < \frac{\pi}{6} (15\%)$



(4) At the interface between on linear magnetic material and another, the magnetic field lines bend. Show that $\frac{\tan \theta_2}{\tan \theta_1} = \frac{\mu_2}{\mu_1}$, assuming no free current at the boundary. (15%)



Time: 150 minutes



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- (5) An infinitely long cylinder of radius *R* carries a "frozen in" magnetization parallel to the cylinder axis $M = ks\hat{z}$. Where *k* is constant and *s* is the distance from the cylinder axis; there is no free current anywhere. Find the magnetic field inside and outside and the cylinder (15%)
- (6) According to quantum mechanics, the current density due to an electron in a hydrogen atom state (n=2, l=2, m=2) is given by

$$\vec{J} = -\frac{1}{2 \cdot 3^8} \frac{e\hbar}{\pi m a^7} r^3 \exp\left(-\frac{2r}{3a}\right) \sin^3 \theta \,\hat{\phi}$$

find the magnetic field at r = 0 (15%)